

MM MM TTTTTTTTTT HH HH DDDDDDDDD CCCCCCCCC 000000 SSSSSSSS HH HH
MM MM TTTTTTTTTT HH HH DDDDDDDDD CCCCCCCCC 000000 SSSSSSSS HH HH
MM MM TT HH HH DD DD CC 00 00 SS HH HH
MM MM TT HH HH DD DD CC 00 00 SS HH HH
MM MM TT HH HH DD DD CC 00 00 SS HH HH
MM MM TT HH HH DD DD CC 00 00 SS HH HH
MM MM TT HHHHHHHHHHHH DD DD CC 00 00 SSSSSS HHHHHHHHHHHH
MM MM TT HHHHHHHHHHHH DD DD CC 00 00 SSSSSS HHHHHHHHHHHH
MM MM TT HH HH DD DD CC 00 00 SS HH HH
MM MM TT HH HH DD DD CC 00 00 SS HH HH
MM MM TT HH HH DD DD CC 00 00 SS HH HH
MM MM TT HH HH DD DD CC 00 00 SS HH HH
MM MM TT HH HH DDDDDDDDD CCCCCCCCC 000000 SSSSSSSS HH HH
MM MM TT HH HH DDDDDDDDD CCCCCCCCC 000000 SSSSSSSS HH HH

(2)	50	HISTORY : Detailed Current Edit History
(3)	86	DECLARATIONS : Declarative Part of Module
(4)	148	MTH\$DCOSH - Standard Double Precision Floating DCOSH

```
0000 1 .TITLE MTH$DCOSH      : Double Floating Hyperbolic Cosine routine
0000 2 .IDENT /1-008/       : (DCOSH)
0000 3 .IDENT /1-008/       : File: MTHDCOSH.MAR Edit: RNH1008
0000 4 :
0000 5 :*****                                                 *
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0000 24 :*
0000 25 :*
0000 26 :*****                                                 *
0000 27 :*
0000 28 :*
0000 29 :* FACILITY: MATH LIBRARY
0000 30 :+
0000 31 :* ABSTRACT:
0000 32 :*
0000 33 :* MTH$DCOSH is a function which returns the double floating hyperbolic cosine
0000 34 :* of its double precision floating point argument. The call is standard
0000 35 :* call-by-reference.
0000 36 :*
0000 37 :-- 
0000 38 :*
0000 39 :* VERSION: 01
0000 40 :*
0000 41 :* HISTORY:
0000 42 :* AUTHOR:
0000 43 :* Peter Yuo, 29-Jun-77: Version 01
0000 44 :*
0000 45 :* MODIFIED BY:
0000 46 :*
0000 47 :*
0000 48 :*
```

0000 50 .SBTTL HISTORY ; Detailed Current Edit History
0000 51
0000 52
0000 53 ; ALGORITHMIC DIFFERENCES FROM FP-11/C ROUTINE: none
0000 54 ;
0000 55 ; Edit History for Version 01 of MTH\$DCOSH
0000 56 ;
0000 57 ; 0-2 MTH\$SError changed to MTH\$SSignal.
0000 58 ; MTH\$... changed to MTH...
0000 59 ; Changed error handling mechanism. Put error result in R0:R1 before
0000 60 ; calling MTH\$SSignal in order to allow user modify error result.
0000 61
0000 62 ; 0-3 Seven term Taylor series, in powers of argument, replaced
0000 63 ; by six term Chebyshev series, in powers of ARG**2,
0000 64 ; with overhang, to improve accuracy, 18-May-1978; Mary Payne
0000 65 ; Fix LOG(2) constant. TNH 16-June-78
0000 66 ; 1-001 - Update version number and copyright notice. JBS 16-NOV-78
0000 67 ; 1-002 - Change MTH_FLOORVEMAT to MTH\$K_FLOORVEMAT. JBS 07-DEC-78
0000 68 ; 1-003 - Removed SSRMDEF - not needed. JBS 16-DEC-78
0000 69 ; 1-004 - Add " to the PSECT directive. JBS 22-DEC-78
0000 70 ; 1-005 - Declare externals. SBL 17-May-1979
0000 71 ; 1-006 - Use MTH\$DEXP R6. SBL 27-Sept-1979
0000 72 ; 1-007 - Changed lower limit for Chebyshev approximation from 2**-27 to
0000 73 ; 2**-28.
0000 74 ; - Eliminated second call to EXP for input values between .25 and
0000 75 ; 28.5*Ln2 by computing COSH(x) = (Z + 1/Z)/2, with Z = EXP(|x|).
0000 76 ; - Eliminated second call to EXP for input values between 28.5*ln2
0000 77 ; and 127*ln2.
0000 78 ; - Changed all final floating point divisions by 2 to integer
0000 79 ; subracts of 1 from the exponent field.
0000 80 ; - Changed entry mask to exclude R7 - no longer needed.
0000 81 ; - Extended maximum range from 87.69 to 128*ln2=88.72.
0000 82 ; - Changed logic for computing EXP(|x|-ln2) to reduce error.
0000 83 ; - RNH 10-FEB-81
0000 84 ; 1-003 - Changed W^ to G^ on call to MTH\$SSignal RNH 09-Sept-1981

```

0000 86 .SBTTL DECLARATIONS ; Declarative Part of Module
0000 87
0000 88 : INCLUDE FILES:
0000 89
0000 90 :
0000 91
0000 92 : EXTERNAL SYMBOLS:
0000 93
0000 94 :
0000 95 .DSABL GBL
0000 96 .EXTRN MTH$DEXP R6
0000 97 .EXTRN MTH$K_FLOORVEMAT
0000 98 .EXTRN MTH$SSIGNAL
0000 99
0000 100 :
0000 101 : EQUATED SYMBOLS:
0000 102
0000 103 SD 1.0 = ^F1.0 : 1.0
0000 104 value = 4 : value.rd.r
0000 105
0000 106 :
0000 107 : MACROS: none
0000 108 :
0000 109 :
0000 110 : PSECT DECLARATIONS:
0000 111
0000 112 .PSECT _MTH$CODE PIC,SHR,LONG,EXE,NOWRT
0000 113 : program section for math routines
0000 114 :
0000 115 : OWN STORAGE: none
0000 116 :
0000 117 :
0000 118 : CONSTANTS:
0000 119 :
0000 120
0000 121 D_127_LOG_2:
0000 122 .QUAD ^X2BDAC7E20F3343B0 : 127*ln2
0008 123 D_128_LOG_2:
0008 124 .QUAD ^XCF79F7D1721743B1 : 128*ln2
0010 125 D_2_POWER_28.5:
0010 126 .QUAD ^XDE6433F904F34EB5 : 2**28.5
0018 127 D_LOG_2_HI:
0018 128 .QUAD ^XCF80F7D172174031 : (high 49 bits of ln2) + 2**-49
0020 129 D_LOG_2_LO:
0020 130 .QUAD ^XFF81898C86C3A5CA : ln2 - D_LOG_2_HI
0028 131
0028 132 DCOSHTAB:
0028 133 .WORD ^0032624,^0024123
002C 134 .WORD ^0037354,^0155722 : DECIMAL: 0.2759648863787355D-06
0030 135 .WORD ^0034320,^0006361
0034 136 .WORD ^0125450,^0145117 : DECIMAL: 0.2480155975461668D-04
0038 137 .WORD ^0035666,^0005540
003C 138 .WORD ^0134001,^0177010 : DECIMAL: 0.138888889781712D-02
0040 139 .WORD ^0037052,^0125252
0044 140 .WORD ^0125252,^0067704 : DECIMAL: 0.416666666665359D-01
0048 141 .WORD ^0040000,0
004C 142 .WORD 0,^0000005 : DECIMAL: 0.5000000000000000D0

```

0000 4080 0050	143	.WORD	^0040200,0	
0000 0000 0054	144	.WORD	0,0	; DECIMAL: 0.100000000000000D+01
00000006 0058	145	DCOSHLEN	= .- DCOSHTAB/8	
0058	146			

```

0058 148      .SBTTL MTH$DCOSH - Standard Double Precision Floating DCOSH
0058 149
0058 150
0058 151 :++
0058 152 : FUNCTIONAL DESCRIPTION:
0058 153
0058 154 : DCOSH - double precision floating point function
0058 155
0058 156 : DCOSH(X) is computed as:
0058 157
0058 158 :   If |X| < 2**-28, DCOSH(X) = 1.
0058 159 :   If 2**-28 <= |X| < 0.25, DCOSH(X) = Chebyshev series
0058 160 :   If 0.25 <= |X| <= 28.5*ln2, set Z = DEXP(|X|) and compute
0058 161 :   DCOSH(X) = (Z + 1/Z)/2.
0058 162 :   If 28.5*ln2 < |X| <= 127*ln2, COSH(X) = EXP(|X|)/2
0058 163 :   If 127*ln2 < |X| <= 128*ln2 then DCOSH(X) = DEXP(|X|-LOG(2)).
0058 164 :   If 128*ln2 < |X| then overflow.
0058 165
0058 166 : CALLING SEQUENCE:
0058 167
0058 168 : DCOSH.wd.v = MTH$DCOSH(x.rd.r)
0058 169
0058 170 : INPUT PARAMETERS:
0058 171
0058 172 :   LONG = 4                                ; define longword multiplier
0058 00000004 173 :   x = 1 * LONG                         ; Contents of x is the argument
0058 174
0058 175 : IMPLICIT INPUTS:    none
0058 176
0058 177 : OUTPUT PARAMETERS:
0058 178
0058 179 :   VALUE: double precision floating hyperbolic cosine of the argument
0058 180
0058 181 : IMPLICIT OUTPUTS:   none
0058 182
0058 183 : COMPLETION CODES:  none
0058 184
0058 185 : SIDE EFFECTS:
0058 186
0058 187 : Signal: MTH$ FLOORVEMAT if 128*ln2 < |X| with reserved operand in R0/R1
0058 188 : (copied to the signal mechanism vector CHFSL_MCH_R0/R1 by LIB$SIGNS).
0058 189 : Associated message is: "FLOATING OVERFLOW IN MATH LIBRARY". Result is reserved
0058 190 : operand -0.0 unless a user supplied (or any) error handler changes CHFSL_MCH_R0/R1
0058 191
0058 192 : NOTE: This procedure disables floating point underflow, enables integer
0058 193 : overflow.
0058 194
0058 195 :---
0058 196
0058 197
407C 198      .ENTRY MTH$DCOSH, ^M<IV, R2, R3, R4, R5, R6 >
005A 199 : standard call-by-reference entry
005A 200 : disable DV (and FU), enable IV
005A 201 MTH$FLAG_JACKET                      ; flag that this is a jacket procedure in
005A
005A      MOVAB  G^MTH$JACKET_HND, (FP)          ; set handler address to jacket
0061
6D 00000000'GF 9E

```

```

0061 ; handler
0061
0061
0061 202
0061 203
0061 204
50 04 BC 70 0061 205 MOVD avalue(AP) R0
50 8000 8F AA 0065 206 BICW2 #^X8000 R0
3F80 8F 50 B1 006A 207 CMPW R0, #^X3F80
14 18 006F 208 BGEQ GEQ_TO_0.25
0071 209
0071 210 : 'X < 0.25
0071 211 : case of an error in routine
0071 212 : If an error, convert signal to user PC
0071 213 : and resignal
0071 214 : R0/R1 = |X| = avalue(AP)
0071 215 : R0/R1 = |X| = avalue(AP)
0071 216 : compare |X| with 0.25
0071 217 : branch if |X| >= 0.25

3280 8F 50 B1 0071 217 CMPW R0, #^X3280
04 18 0076 218 BGEQ GEQ_TO_2M28
0078 219 : compare |X| with 2**-28
0078 220 : branch if |X| >= 2**-28

0078 221 MOVD S^#SD_1.0, R0
50 08 70 0078 222 RET
04 0078 223
007C 224 : R0/R1 = 1.0
007C 225 : return with result = 1.0
007C 226 :
007C 227 :
007C 228 GEQ_TO_2M28:
007C 229 MULD R0,R0
50 50 64 007C 230 POLYD R0, #DCOSHLEN-1, DCOSHTAB
A4 AF 05 50 75 007F 231 : Get ARG**2 for POLYD.
0084 232 RET : R0/R1 = SUM(Ci*X**i)
04 0084 233 : return with result in R0

0085 234 :
0085 235 : 0.25 < |X|
0085 236 :
0085 237 :
0085 238 GEQ_TO_0.25:
FF76 CF 50 71 0085 239 CMPD R0, D 127 LOG 2
1A 14 008A 240 BGTR GTR_TRAN_T27_LOG_2
008C 241
008C 242 : compare |X| with 127*ln2
008C 243 : branch if |X| > 127*ln2
008C 244 :
008C 245 :
00000000'EF 16 008C 246 JSB MTH$DEXP R6
FF79 CF 50 71 0092 247 CMPD R0, D 2 POWER_28.5
07 14 0097 248 BGTR ONE_TERM ONLY
52 08 50 67 0099 249 DIVD3 R0, S^#SD_1.0, R2
50 52 60 009D 250 ADDD R2, R0
00A0 251 ONE_TERM ONLY:
50 0080 8F A2 00A0 252 SUBW #^X0080, R0
04 00A5 253 RET : R0/R1 = (DEXP(X) + DEXP(-X))/2
00A6 254
00A6 255 : return with result in R0/R1
00A6 256 : 127*ln2 < |X|

```

```

00A6 257 :
00A6 258
00A6 259 GTR_THAN_127_LOG_2:
FF5D CF 50 71 00A6 260 CMPD R0, D_128_LOG_2      : Check for possible overflow
15 14 00AB 261 BGTR ERROR
50 FF67 CF 62 00AD 262 SUBD D_LOG_2_HI, R0
00000000'EF 16 00B2 263 JSB MTH$DEXP_R6
52 50 FF64 CF 65 00B8 264 MULD3 D_LOG_2_E0, R0, R2
50 52 62 00BE 265 SUBD R2, R0
04 00C1 266 RET
00C2 267 :
00C2 268 : 128*ln2 < ix:
00C2 269 :
00C2 270
7E 00'8F 9A 00C2 271 ERROR: MOVZBL #MTH$K_FLOORVEMAT, -(SP) ; condition value
50 01 0F 79 00C6 272 ASHQ #15, #T, R0      : R0 = result = reserved operand -0.0
00CA 273
00CA 274
00CA 275
00000000'GF 01 FB 00CA 276 CALLS #1, G^MTH$SSIGNAL ; goes to signal mechanism vector
00D1 277
04 00D1 278 RET      : (CHFSL_MCH_R0/R1) so error handler
00D2 279
00D2 280
00D2 281
00D2 282 .END

```

DCOSHLEN	= 00000006
DCOSHTAB	00000028 R 01
D_127_LOG_2	00000000 R 01
D_-128_LOG_2	00000008 R 01
D_-2_POWER_-28.5	00000010 R 01
D_LOG_2_HI	00000018 R 01
D_LOG_2_LO	00000020 R 01
ERROR	000000C2 R 01
GEO_TO_0.25	00000085 R 01
GEO_TO_2M28	0000007C R 01
GTR_THAN_127_LOG_2	000000A6 R 01
LONG	= 00000004
MTH\$S\$JACKET_HND	***** X 01
MTH\$S\$SIGNAL	***** X 00
MTH\$DCOSH	00000058 RG 01
MTH\$DEXP R6	***** X 00
MTH\$K_FLOORMAT	***** X 00
ONE_TERM_ONLY	000000A0 R 01
SD_T_0	= 00004080
VALUE	= 00000004

-----+
! Psect synopsis !
-----+

Psect name	Allocation	Psect No.	Attributes	CON	ABS	LCL	NOSHR	NOEXE	NORD	NOWRT	NOVEC	BYTE
ABS	00000000 (0.)	00 (0.)	NOPIC USR	CON	ABS	LCL	NOSHR	NOEXE	NORD	NOWRT	NOVEC	BYTE
_MTH\$CODE	000000D2 (210.)	01 (1.)	PIC USR	CON	REL	LCL	SHR	EXE	RD	NOWRT	NOVEC	LONG

-----+
! Performance indicators !
-----+

Phase	Page faults	CPU Time	Elapsed Time
Initialization	32	00:00:00.10	00:00:00.72
Command processing	119	00:00:00.66	00:00:04.63
Pass 1	92	00:00:00.90	00:00:04.19
Symbol table sort	0	00:00:00.01	00:00:00.00
Pass 2	65	00:00:00.70	00:00:02.47
Symbol table output	3	00:00:00.03	00:00:00.08
Psect synopsis output	3	00:00:00.02	00:00:00.02
Cross-reference output	0	00:00:00.00	00:00:00.00
Assembler run totals	316	00:00:02.42	00:00:12.12

The working set limit was 750 pages.

4120 bytes (9 pages) of virtual memory were used to buffer the intermediate code.

There were 10 pages of symbol table space allocated to hold 21 non-local and 0 local symbols.

342 source lines were read in Pass 1, producing 11 object records in Pass 2.

1 page of virtual memory was used to define 1 macro.

Macro library statistics

Macro library name

Macros defined

-\$2553DUA28:[SYSLIB]STARLET.MLB;2

0

0 GETS were required to define 0 macros.

There were no errors, warnings or information messages.

MACRO/ENABLE=SUPPRESSION/DISABLE=(GLOBAL,TRACEBACK)/LIS=LIS\$:MTHDCOSH/OBJ=OBJ\$:MTHDCOSH MSRC\$:MTHJACKET/UPDATE=(ENHS:MTHJACKET)+MSRC

MTH
Sym
ACM
APP
DXP
DXP
DXP
DXP
D-1
D-L
D-L
EVA
EXC
LON
MTH
OVE
SF\$
SMT
TAB
TAB
UND
X
X-2

PSE
—

5
SAB
MT

Pha

Ini
Com
Pas
Sym
Pas
Sym
Pse
Cra

The
860

0259 AH-BT13A-SE
VAX/VMS V4.0

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